

*Lecture 2 362 January 16, 2019*

*Paradigm Shift:  
Development of Current  
Atomic Theory—  
Spectroscopy and Energy  
Levels in Atoms*

*OR,  
“Show me the Electrons!”*

Color	Metal Flame Colors
Red	<p><i>Carmines</i>: Lithium compounds. Masked by barium or sodium.</p> <p><i>Scarlet or Crimson</i>: Strontium compounds. Masked by barium.</p> <p><i>Yellow-Red</i>: Calcium compounds. Masked by barium.</p>
Yellow	Sodium compounds, even in trace amounts. A yellow flame is not indicative of sodium unless it persists and is not intensified by addition of 1% NaCl to the dry compound.
White	<i>White-Green</i> : Zinc
Green	<p><i>Emerald</i>: Copper compounds, other than halides. Thallium.</p> <p><i>Blue-Green</i>: Phosphates, when moistened with <math>\text{H}_2\text{SO}_4</math> or <math>\text{B}_2\text{O}_3</math>.</p> <p><i>Faint Green</i>: Antimony and <math>\text{NH}_4</math> compounds.</p> <p><i>Yellow-Green</i>: Barium, molybdenum.</p>
Blue	<p><i>Azure</i>: Lead, selenium, bismuth, <math>\text{CuCl}_2</math> and other copper compounds moistened with hydrochloric acid.</p> <p><i>Light Blue</i>: Arsenic and some of its compounds.</p> <p><i>Greenish Blue</i>: <math>\text{CuBr}_2</math>, antimony</p>
Violet	<p>Potassium compounds other than borates, phosphates, and silicates. Masked by sodium or lithium.</p> <p><i>Purple-Red</i>: Potassium, rubidium, and/or cesium in the presence of sodium when viewed through a blue glass.</p>

# ***Atomic Emission (Spectroscopy)***

- An emission spectrum requires first the addition of energy to a material.
- The addition of energy promotes electrons of that material from the ground state to the excited state.
- As the electrons “fall” from the excited state to the ground state, they emit the energy they absorbed in the form of electromagnetic radiation (heat, light, etc.)

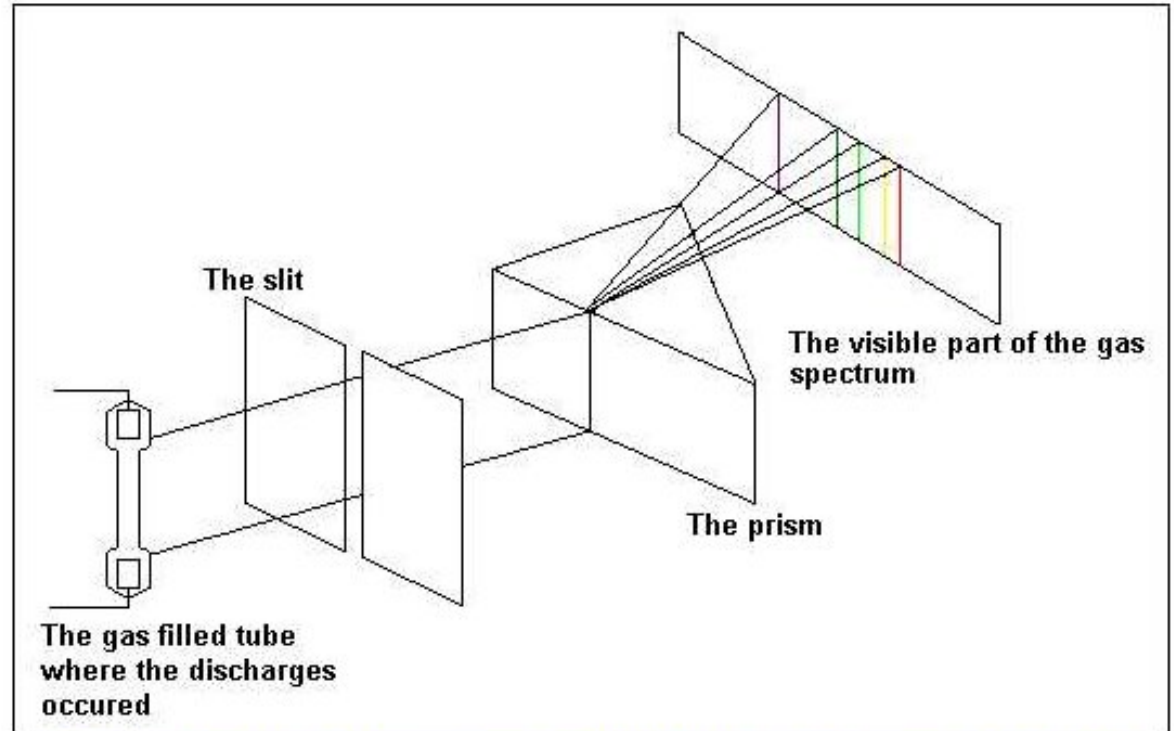
## **Comments**

- Atomic emission is used in street lamps, fluorescent lights, and neon signs.
- Two common street lamps using this are the mercury lamp and the sodium lamp.
- “Neon” signs frequently implement the emission spectra of other gases such as argon and krypton.
- Very sophisticated instrumental techniques such as “flame photometry” and “atomic absorption” are based on the principles of atomic emission.

# Continuous and Line Spectra



Dark Side of the Moon  
Pink Floyd



The discharges in the low pressure gas filled tube are the sources of the light which undergo refraction on the prism. We see the line spectrum of the gas.

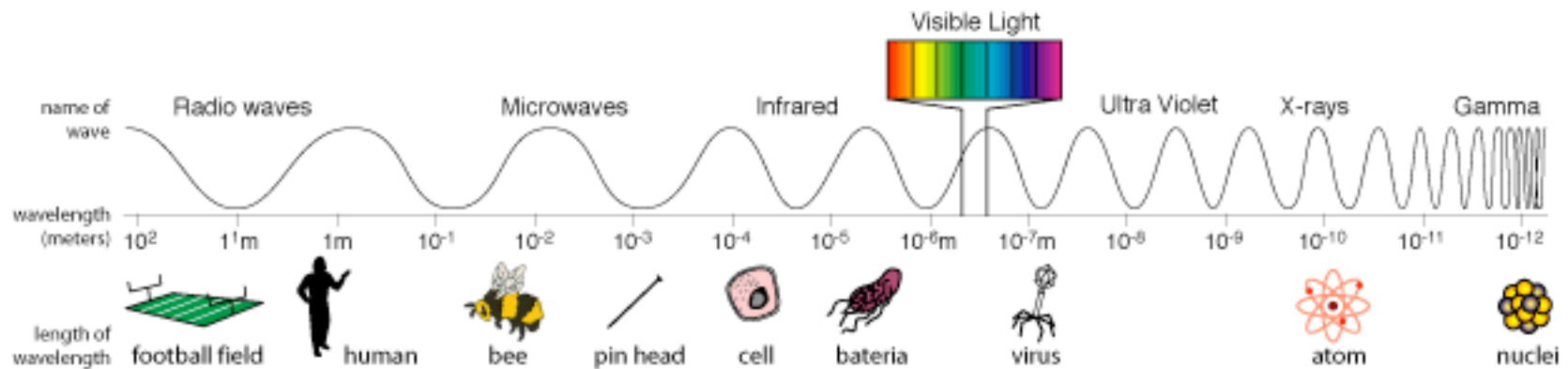
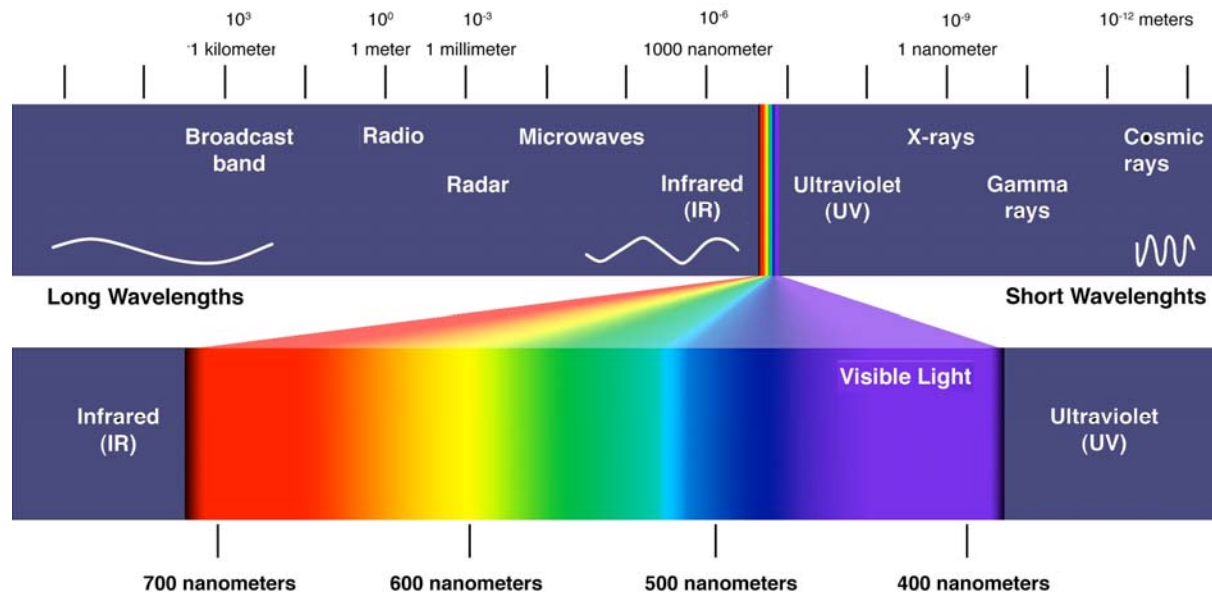
## Sodium Flame Spectrum

<http://webmineral.com/help/FlameTest.shtml>



Both neutral and singly ionized sodium contribute to the emission lines in this spectrum.

# Electromagnetic Radiation Spectrum



***In the news: January 20, 2016: Infer what we cannot see. . .***

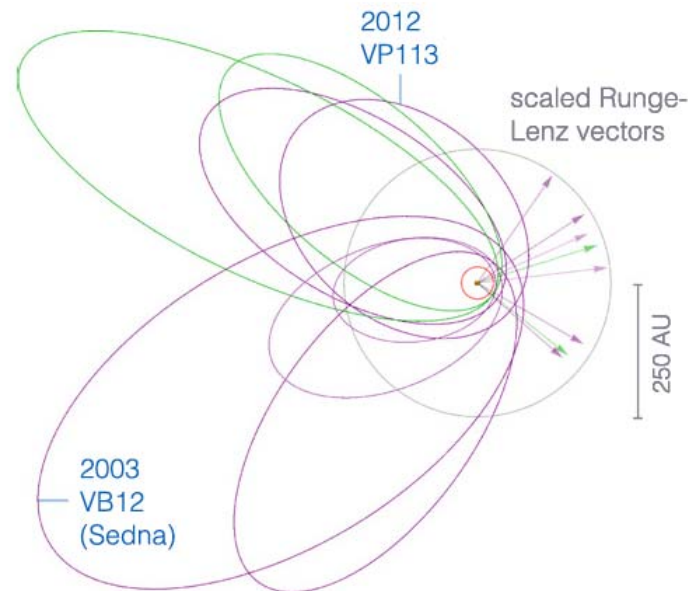
## EVIDENCE FOR A DISTANT GIANT PLANET IN THE SOLAR SYSTEM

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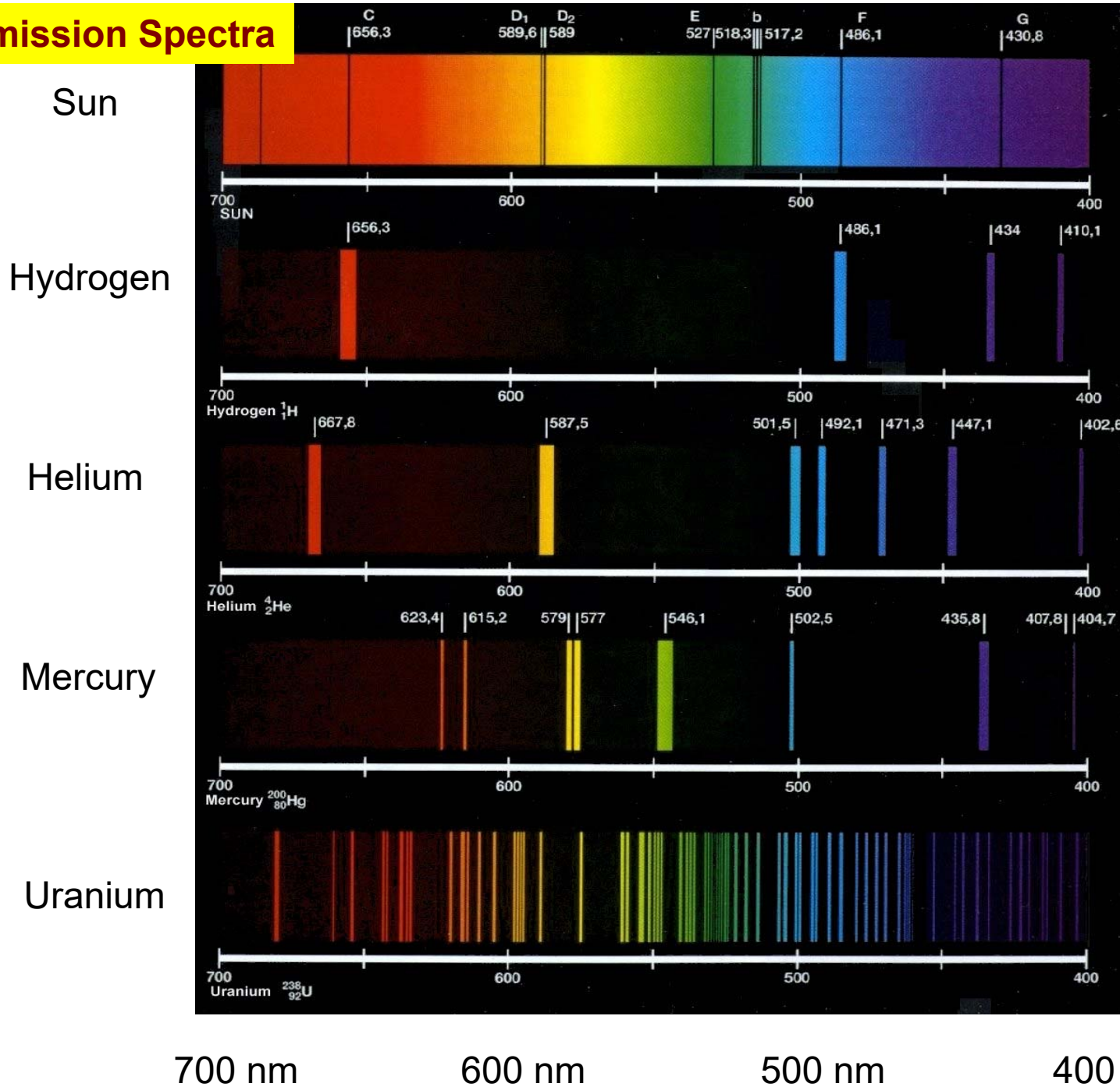
*Received 2015 November 13; accepted 2016 January 10; published 2016 January 20*

BATYGIN & BROWN



Cumulatively, the presented results offer credence to the hypothesis that the observed structure of the distant Kuiper Belt can be explained by invoking perturbations from an unseen planetary mass companion to the solar system. Simultaneously, the suggestive nature of the results should be met with a healthy dose of skepticism, given the numerous assumptions made in the construction of our simple analytical model. In

# Emission Spectra



*Complexity increases  
With size of  
Element*

*What do these lines  
mean?????*

700 nm                      600 nm                      500 nm                      400 nm

# A Bit of History

**TABLE 2.1 Discoveries in Atomic Structure**

1896	A. H. Becquerel	Discovered radioactivity of uranium
1897	J. J. Thomson	Showed that electrons have a negative charge, with charge/mass = $1.76 \times 10^{11}$ C/kg
1909	R. A. Millikan	Measured the electronic charge as $1.60 \times 10^{-19}$ C; therefore, mass of electron = $9.11 \times 10^{-31}$ kg
1911	E. Rutherford	Established the nuclear model of the atom: a very small, heavy nucleus surrounded by mostly empty space
1913	H. G. J. Moseley	Determined nuclear charges by X-ray emission, establishing atomic numbers as more fundamental than atomic masses



Z = No. protons in nucleus, Atomic number

A = Mass number; no. of protons + neutrons in nucleus



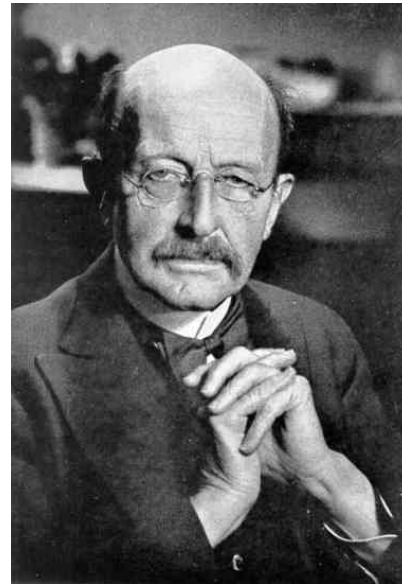


Marie Curie—1867-1934

So how to connect the physical properties of elements to the Periodic Table? Physicists! The current model of the atom belongs to Physicists!



DeBroglie



Planck



Schrodinger



Einstein



Heisenberg



Bohr

Pauli



## Niels Bohr and wife Margrethe around 1930

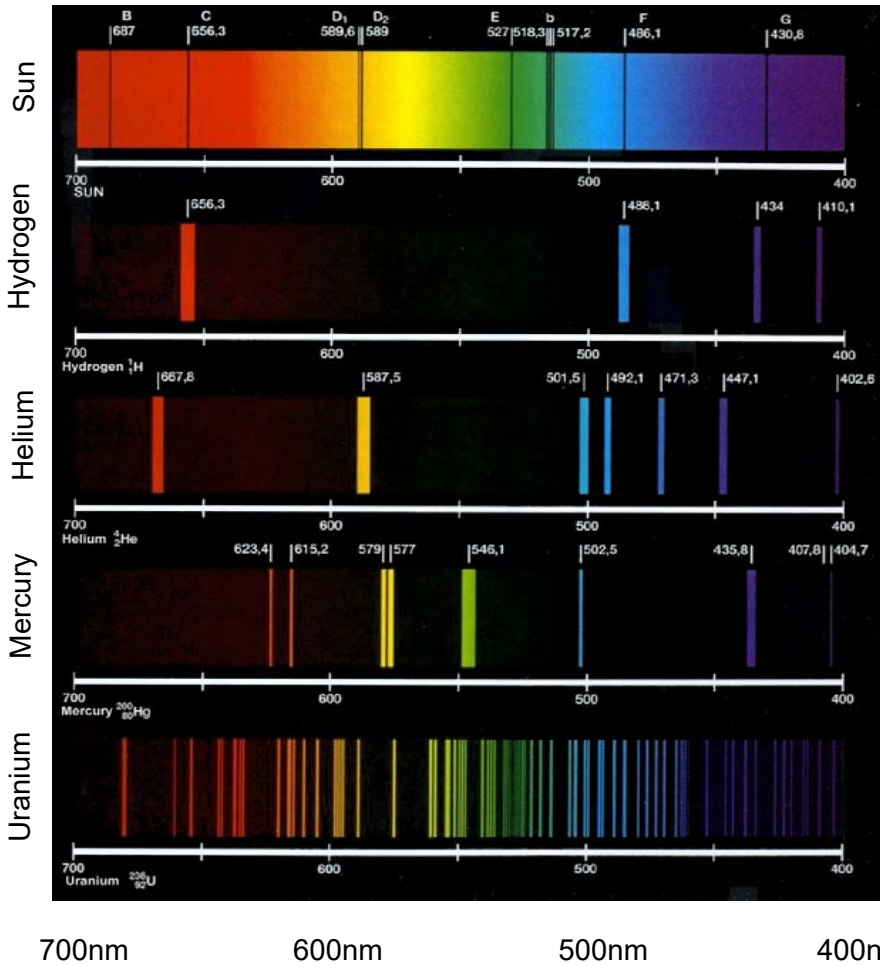


Taken from John L. Heilbron's "History: The Path to the quantum Atom",  
Nature 498, 27-30, (06 June 2013)

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Nature 498, 27-30, (06 June 2013)

To develop his model, Bohr followed an analogy to the radiation theory of Max Planck (right). ". . . Bohr had developed a doctrine of multiple partial truths, each of which contained some bit of reality, and all of which together might exhaust it. "There exist so many different truths I can almost call it my religion that I think that everything that is of value is true."

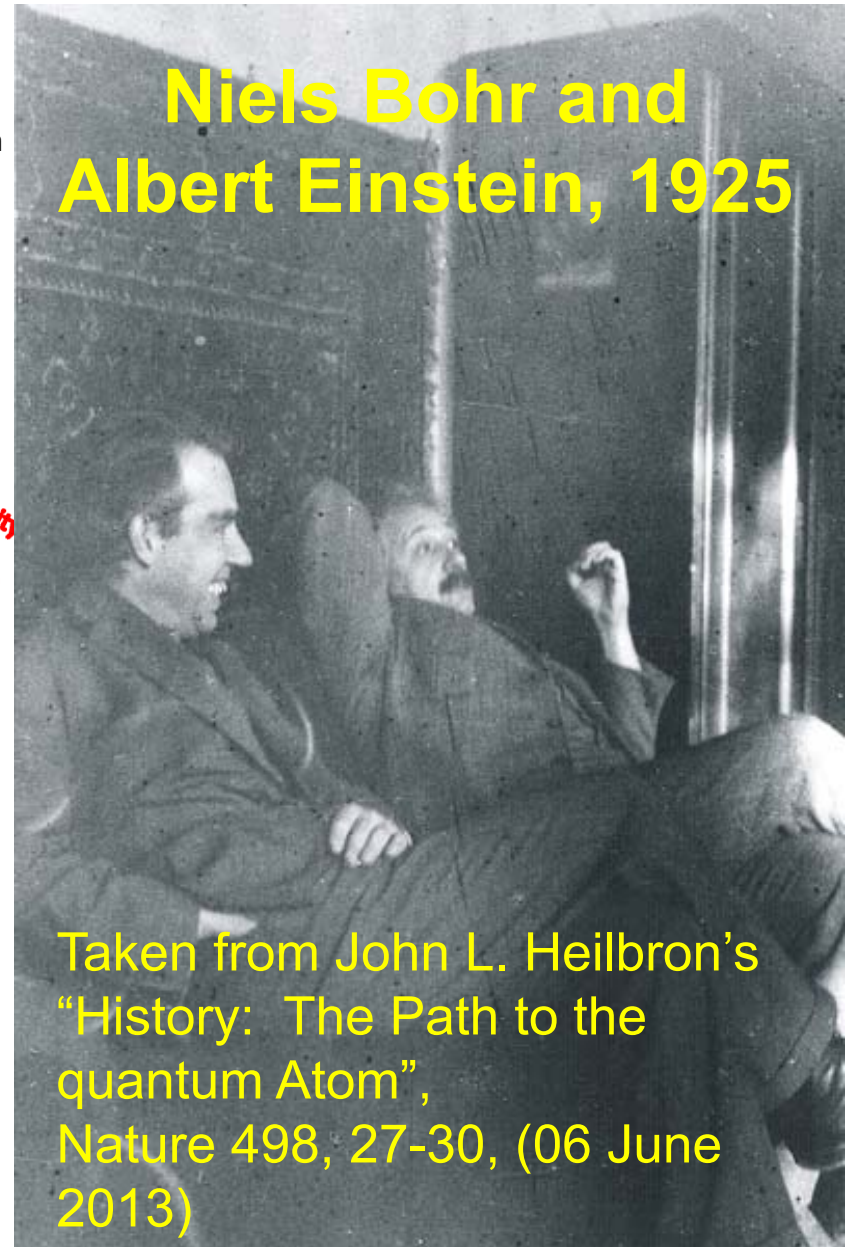




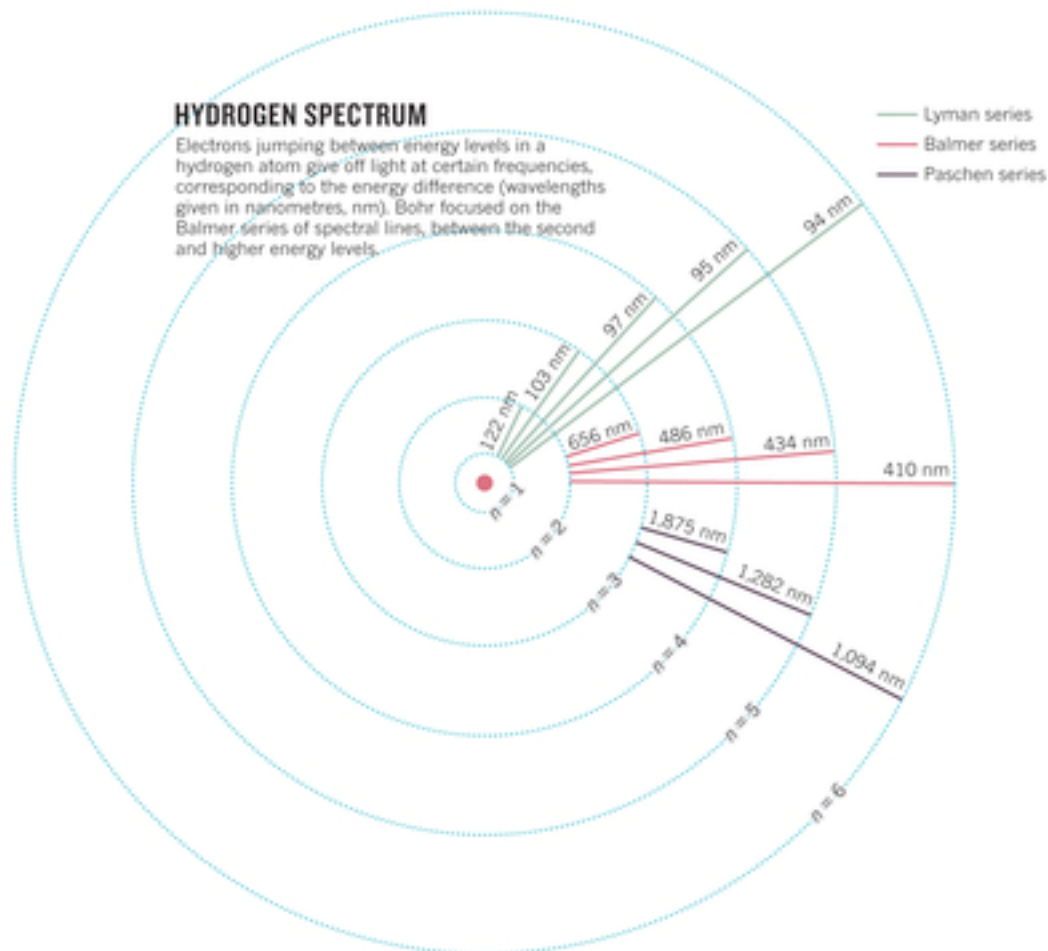
Emission Spectra

*Complexity increases with size of Element*

*What do these lines mean?????*



# The Bohr Atom: electrons in concentric rings



Taken from John L. Heilbron's "History: The Path to the quantum Atom",  
Nature 498, 27-30, (06 June 2013)

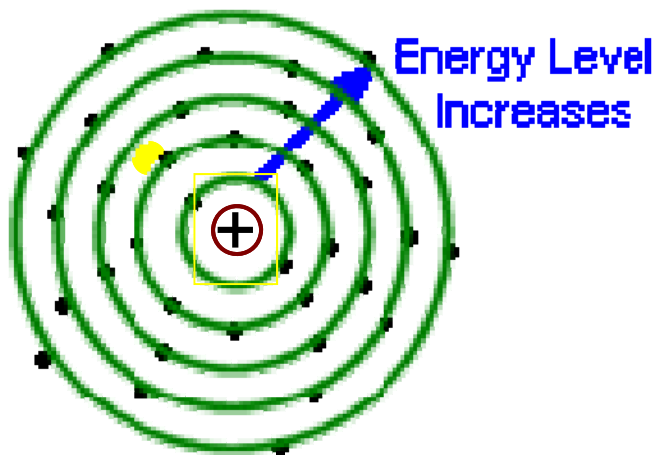
The Balmer formula expresses the frequencies of some lines in the spectrum of hydrogen in simple algebra:

$$\nu_n = R(1/2^2 - 1/n^2)$$

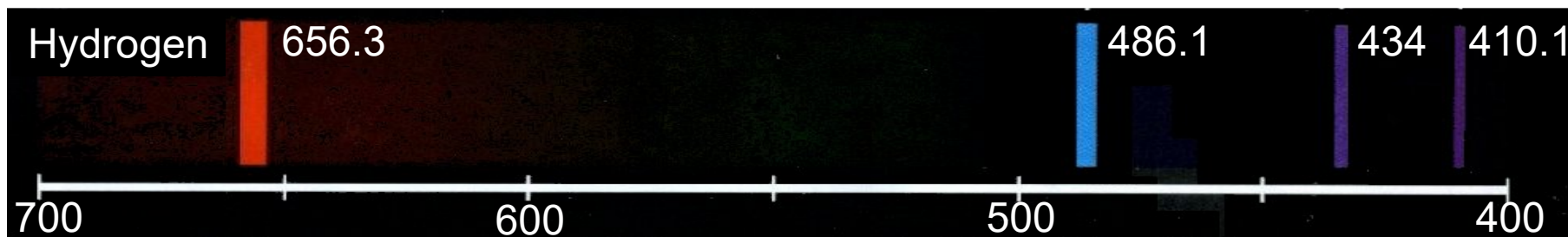
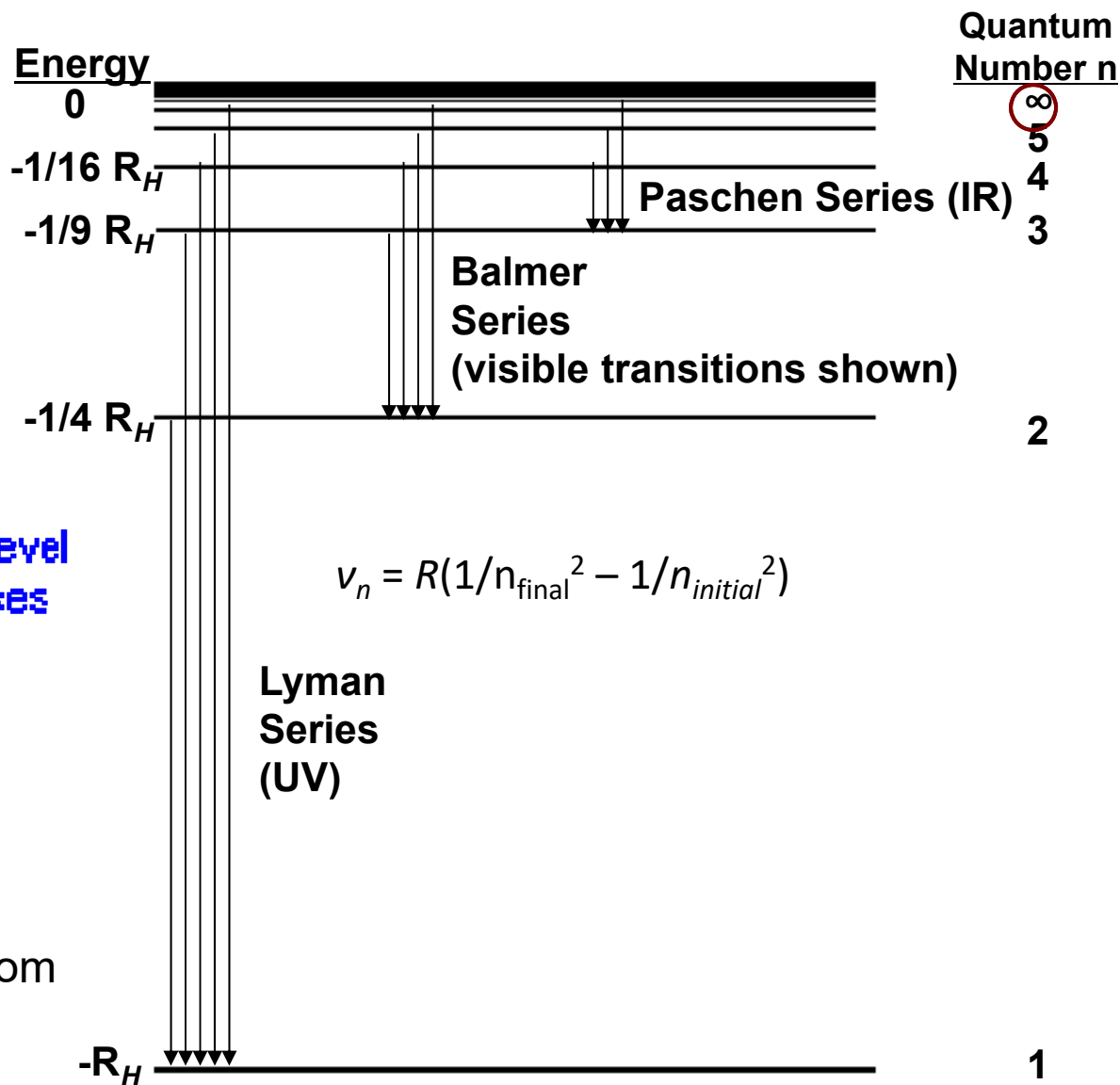
where  $\nu_n$  is the  $n$ th Balmer line and  $R$  is the universal Rydberg constant for frequency, named in honour of the Swedish spectroscopist Johannes Rydberg, who generalized Balmer's formula to apply to elements beyond hydrogen.

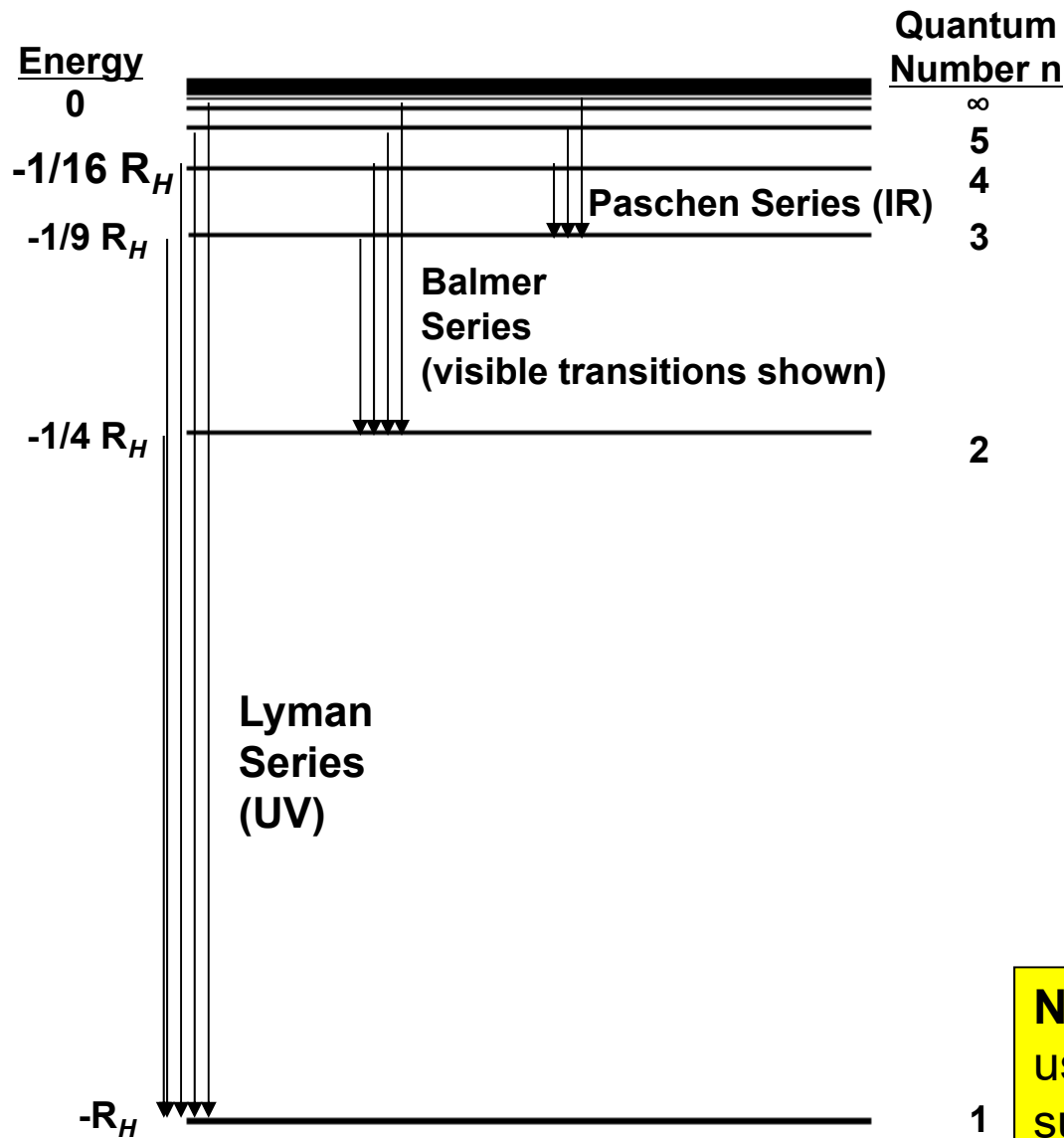
**Each level can accommodate  $2n^2$  electron:**  
**Periodic Table Rows**

# The Hydrogen Atom Spectrum and Energy Levels



Niels Bohr's view of the atom





For Hydrogen:

$$E = \frac{-R_H}{n^2}$$

Rydberg constant for hydrogen,  $R_H$

$$R_H = \frac{m_e e^4}{8 \epsilon_0^2 h^2} = 2.179 \times 10^{-18} \text{ J}$$

$$= 13.6 \text{ eV}$$

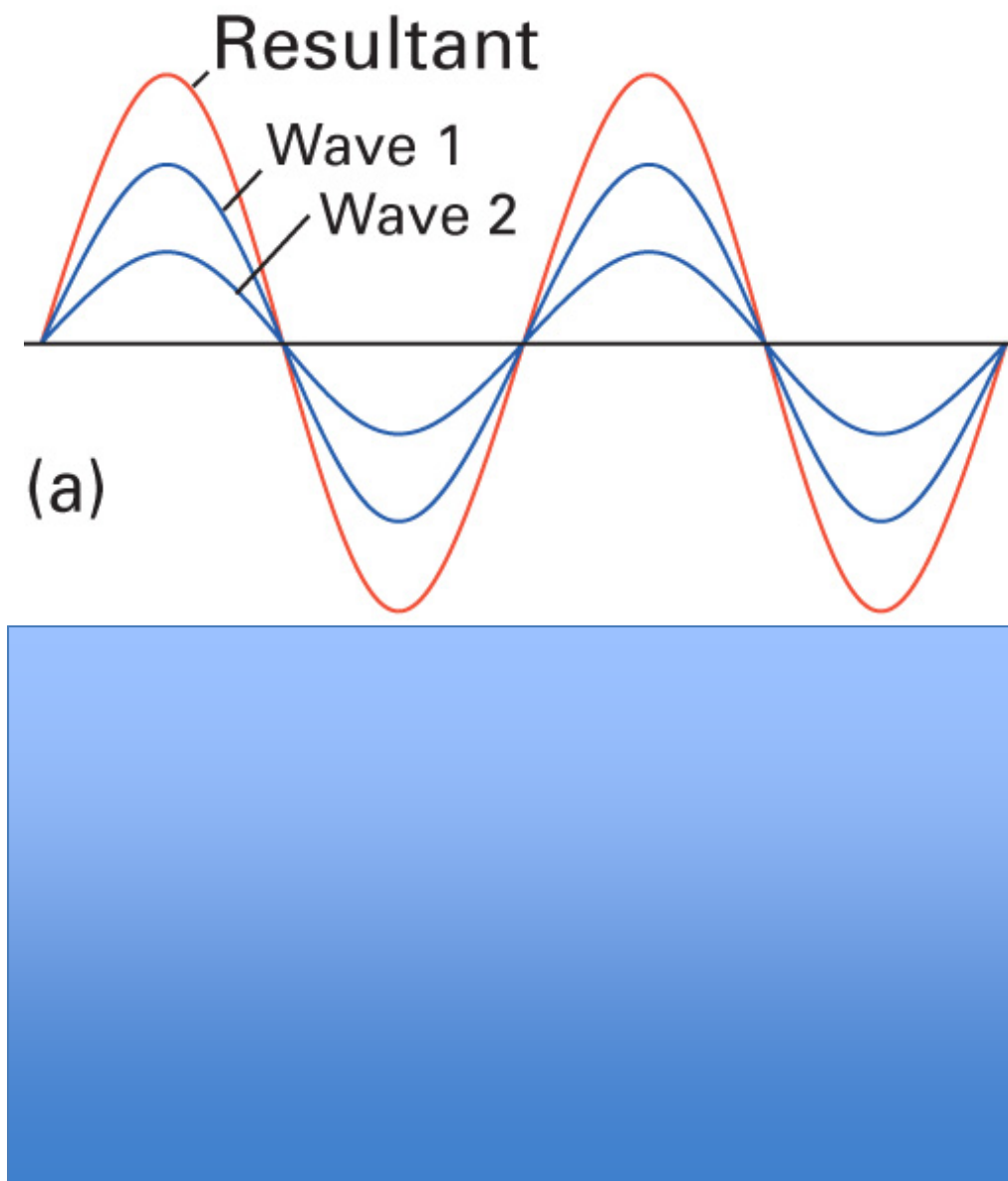
General equation for Rydberg constant for any element

$$R = \frac{-\mu Z^2 e^4}{8 \epsilon_0^2 h^2}$$

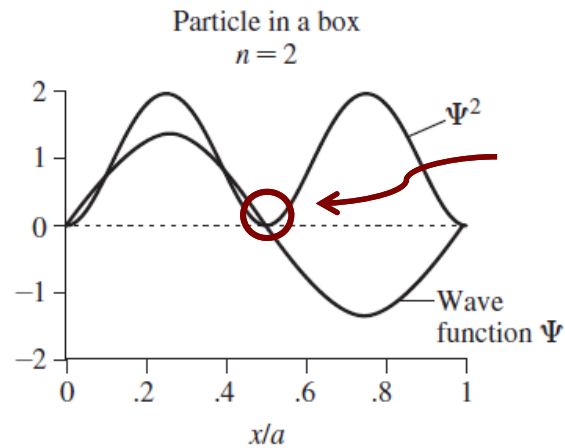
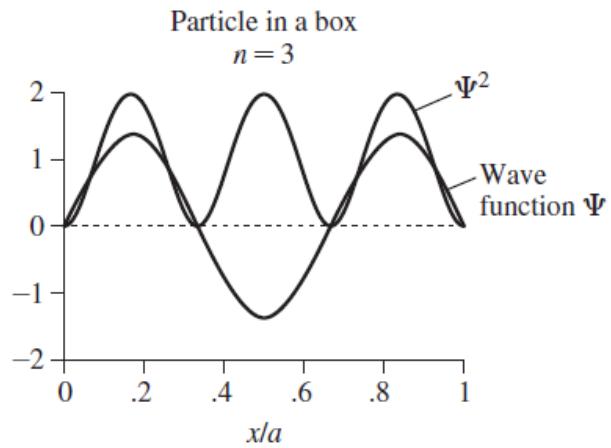
**Note:** The predicted emission spectra using the Rydberg constant was only successful for simple elements such as H and failed for heavier atoms due to the limitations of the Bohr view of the atom. ***This led to the foundations of quantum mechanics.***



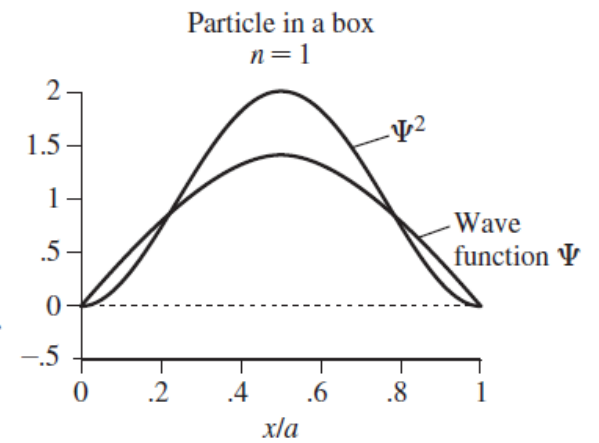
**Properties of waves: Addition for reinforcement or cancellation**



# Properties of waves: Squared = amplitude Boundaries => Restrictions on values

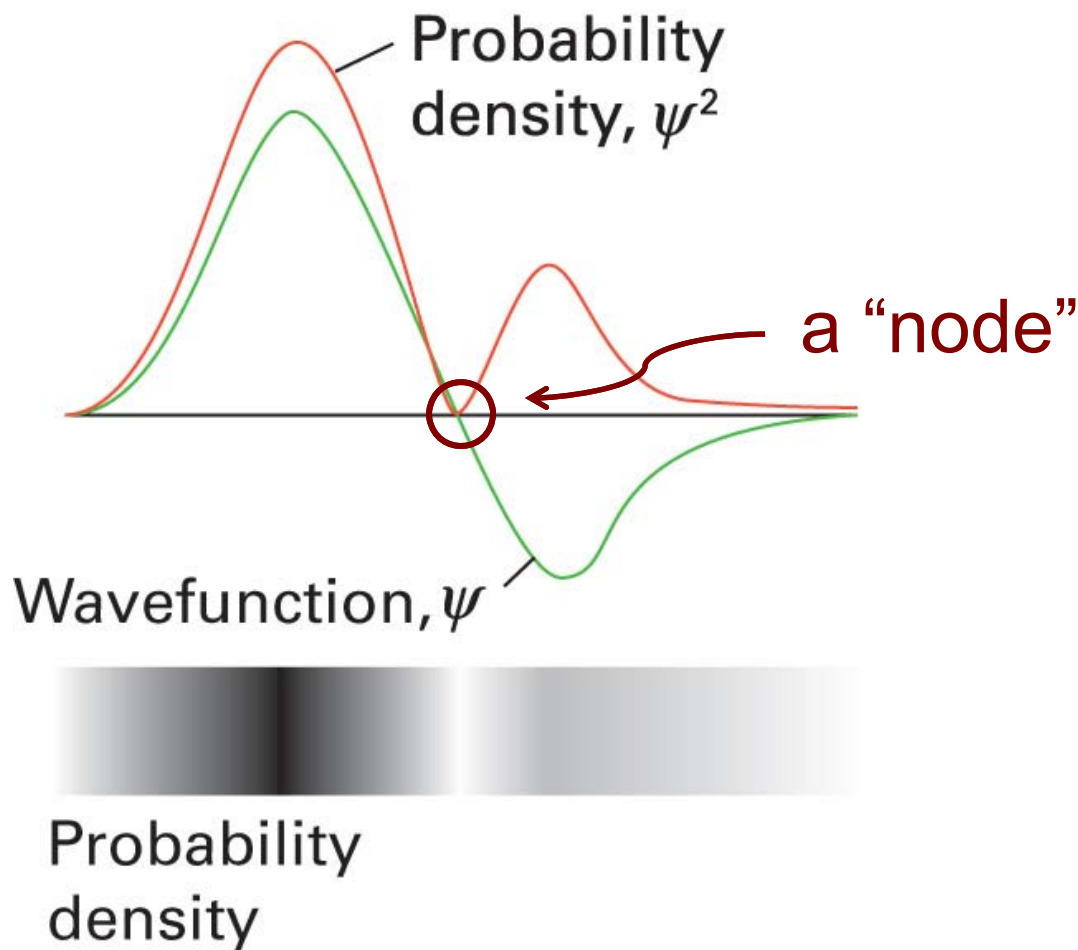


a "node"

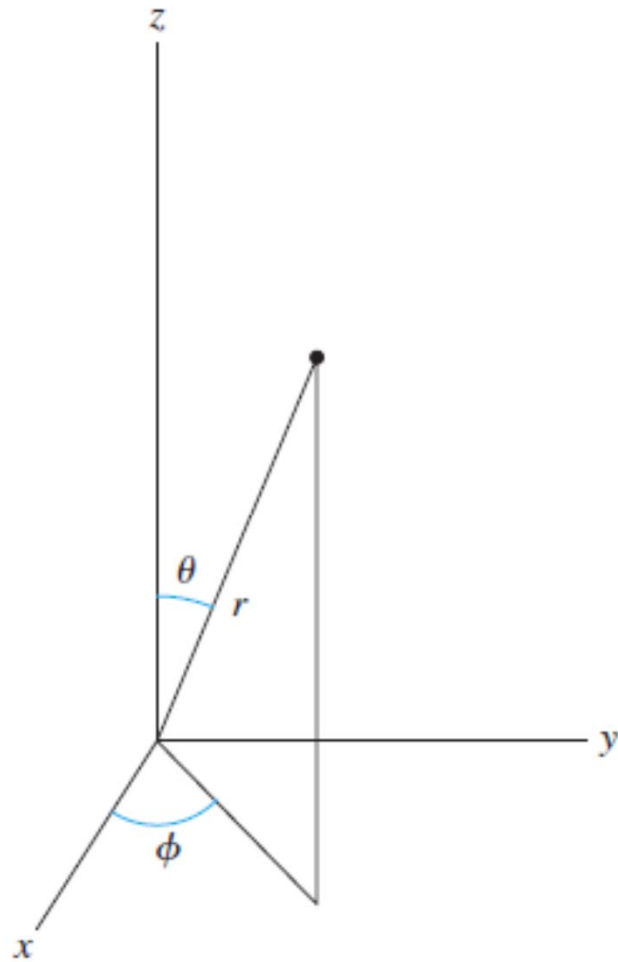


Time-independent Schrödinger equation  
(general—one dimension)

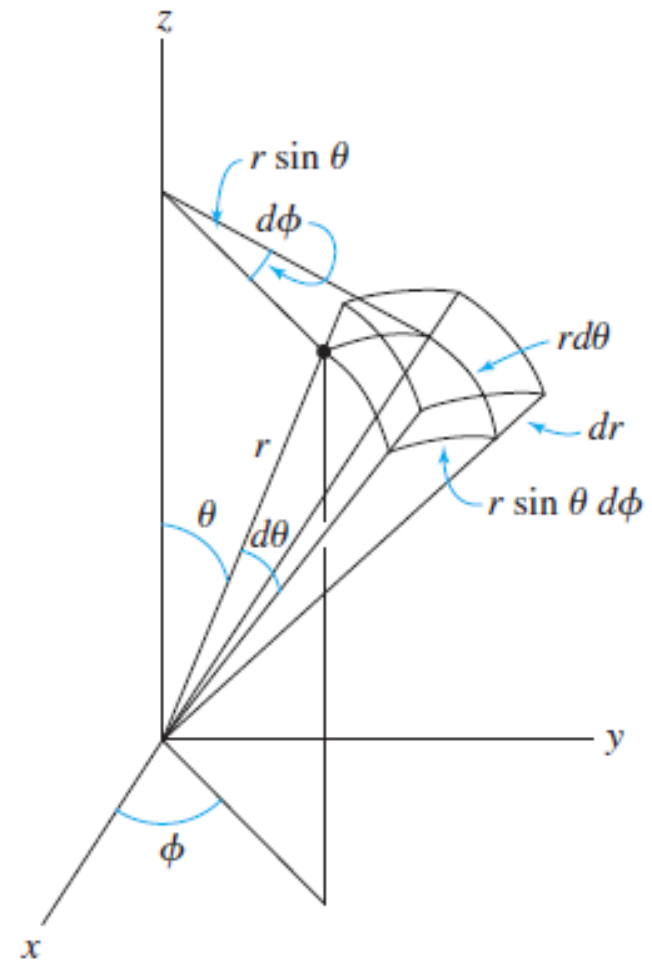
$$\hat{H}\psi = E\psi$$



# Need for Spherical Coordinates and Volume Elements

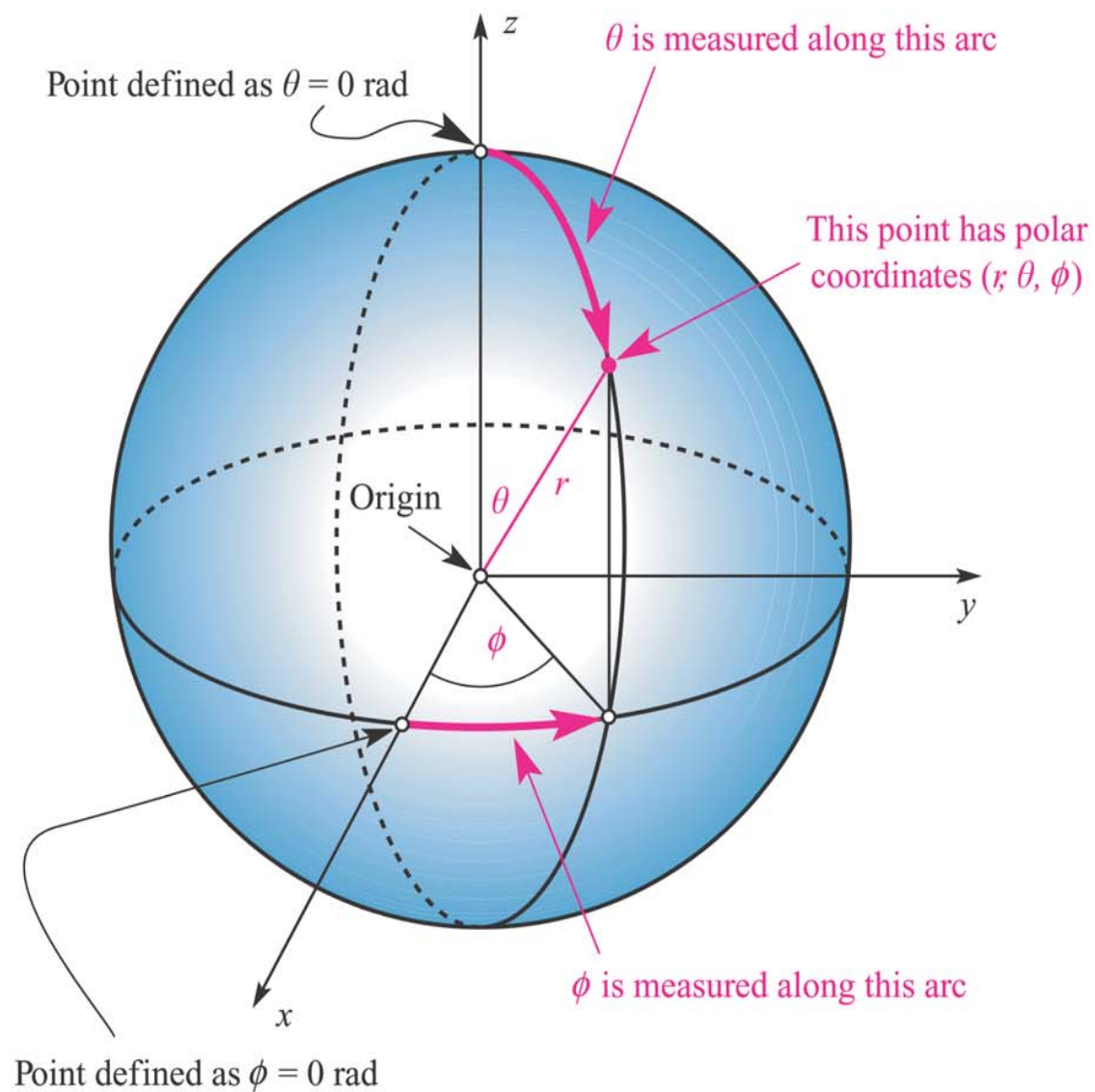


Spherical coordinates



Volume element

**Need both radial and angular functions**



**Fig. 1.4** Definition of the polar coordinates  $(r, \theta, \phi)$  for a point shown here in pink;  $r$  is the radial coordinate and  $\theta$  and  $\phi$  are angular coordinates.  $\theta$  and  $\phi$  are measured in radians (rad). Cartesian axes ( $x$ ,  $y$  and  $z$ ) are also shown.

## Summarizing: Solutions Required Quantum Numbers

### Quantum Numbers

Atomic orbital	$n$	$l$	$m_l$	Radial part of the wavefunction, $R(r)^\dagger$	Angular part of wavefunction, $A(\theta, \phi)$
$1s$	1	0	0	$2e^{-r}$	$\frac{1}{2\sqrt{\pi}}$
$2s$	2	0	0	$\frac{1}{2\sqrt{2}}(2-r)e^{-r/2}$	$\frac{1}{2\sqrt{\pi}}$
$2p_x$	2	1	+1	$\frac{1}{2\sqrt{6}}re^{-r/2}$	$\frac{\sqrt{3}(\sin\theta\cos\phi)}{2\sqrt{\pi}}$
$2p_z$	2	1	0	$\frac{1}{2\sqrt{6}}re^{-r/2}$	$\frac{\sqrt{3}(\cos\theta)}{2\sqrt{\pi}}$
$2p_y$	2	1	-1	$\frac{1}{2\sqrt{6}}re^{-r/2}$	$\frac{\sqrt{3}(\sin\theta\sin\phi)}{2\sqrt{\pi}}$

<sup>†</sup> For the  $1s$  atomic orbital, the formula for  $R(r)$  is actually  $2\left(\frac{Z}{a_0}\right)^{3/2}e^{-Zr/a_0}$  but for the hydrogen atom,  $Z = 1$  and  $a_0 = 1$  atomic unit. Other functions are similarly simplified.

**Table 1.2** Solutions of the Schrödinger equation for the hydrogen atom which define the  $1s$ ,  $2s$  and  $2p$  atomic orbitals. For these forms of the solutions, the distance  $r$  from the nucleus is measured in atomic units.

*Lecture 3 362 January 18, 2019*

*Quantum Numbers*  
*Effective Nuclear Charge*  
*Slater's Rules*

*Lecture 2 362 January 16, 2019*

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Development of Current  
Atomic Theory—  
Spectroscopy and Energy  
Levels in Atoms*

*OR,  
“Show me the Electrons!”*